

EE 313 – Problem Set 1

Material to be covered on Quiz 1 scheduled September 12th

1. For the following pairs of signals, make a determination about which signal leads by a positive angle.

- a. $v_1(t) = 4 \cos(5t)$ Volts and $v_2(t) = 10 \cos(5t-20^\circ)$ Volts
- b. $v_x(t) = -10 \cos(100t+50^\circ)$ Volts and $v_y(t) = 10 \sin(100t+10^\circ)$ Volts
- c. $i_x(t) = -2 \sin(t-130^\circ)$ Amps and $i_y(t) = -5 \cos(t+100^\circ)$ Amps

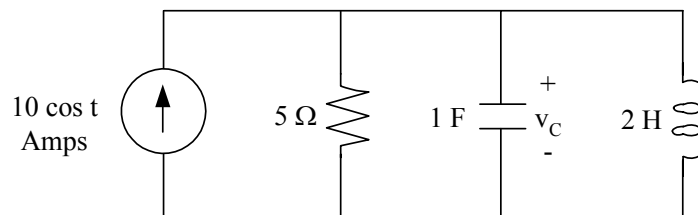
2. Transform the following sinusoidal time functions into the complex exponential form and then into the phasor form.

- a. $v(t) = 10 \cos(120t-225^\circ)$ Volts
- b. $i(t) = 5 \sin(600t-125^\circ)$ Amps
- c. $v(t) = -3 \sin(20t)$ Volts
- d. $i(t) = -10 \cos(2t+45^\circ)$ Amps

3. Evaluate the following expressions and transform them into the sinusoidal time representation. Your final answer should be in the following form: $f(t) = A \cos(\omega t + \phi) + jB \sin(\omega t + \phi)$. For each answer below, the angular frequency is 5 rad/s.

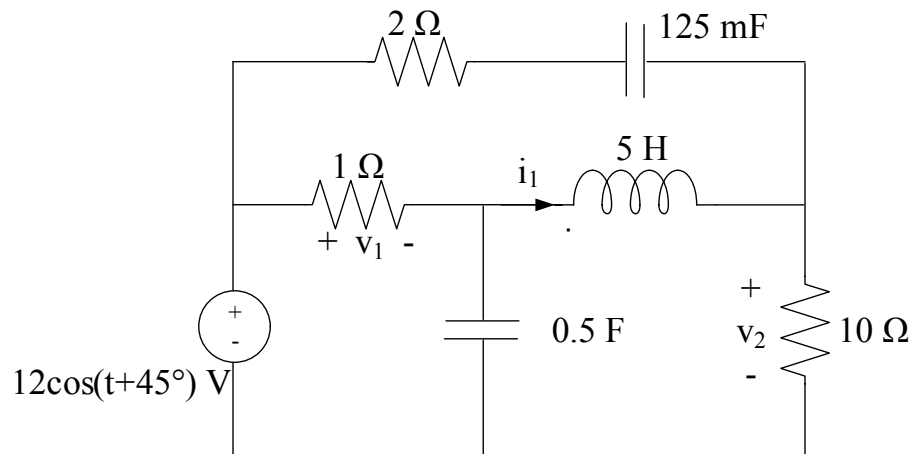
- a. $6\angle 25^\circ + 10\angle -40^\circ$
- b. $(5\angle 80^\circ)(2+j4)$
- c. $(-1-j8) + (6+j5)$
- d. $(2\angle 140^\circ) + (3-j6)$
- e. $\frac{(-4+j3)}{2\angle 10^\circ}$
- f. $\frac{10\angle -25^\circ}{-2+j10}$

4. Consider the following circuit.



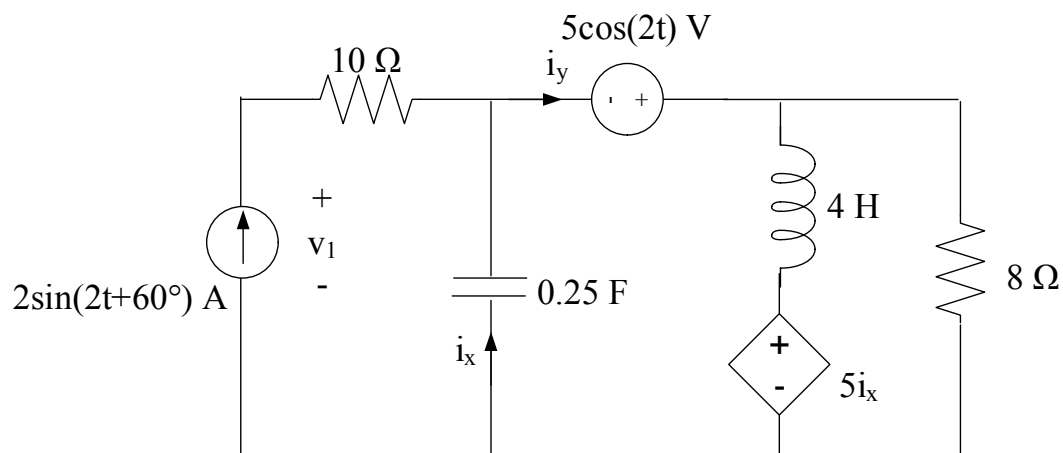
- a. Find the forced response for $v_C(t)$. The solution guess is $v_C(t) = A\cos(t) + B\sin(t)$.
- b. Find the forced response for $v_C(t)$. The solution guess is $v_C(t) = Ae^{jt}$.

5. The following circuit is given in the time domain and assumes steady-state conditions:



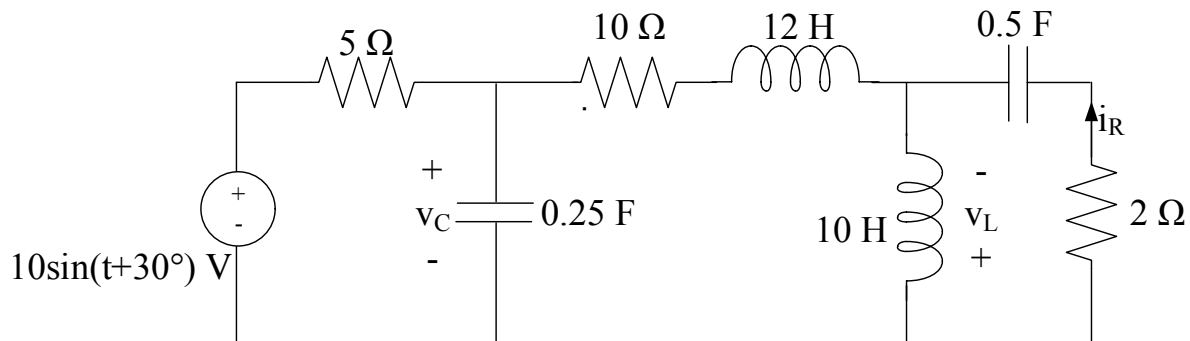
- Transform the circuit to the frequency domain.
- Use nodal analysis and mesh analysis to solve for the phasor voltages, \mathbf{V}_1 and \mathbf{V}_2 and the phasor current, \mathbf{I}_1 . Show that your answers for each method match.
- Transform the phasors to the time domain and give the real part of the sinusoidal representation.

6. The following circuit is given in the time domain and assumes steady-state conditions:



- Transform the circuit to the frequency domain.
- Using nodal analysis and mesh analysis, solve for the phasors \mathbf{V}_1 and \mathbf{I}_x and \mathbf{I}_y .
- Find $v_1(t)$ and $i_x(t)$ and $i_y(t)$ (only the real part of the signal is necessary).

7. Consider the following subcircuit.



- Convert the circuit from the time domain to the frequency domain.
- Find the equivalent impedance seen by the source. What is the reactance of the impedance? Is it capacitive or inductive?
- Expand the circuit and find the labeled voltages and current in phasor form and then give the real part of time domain values.