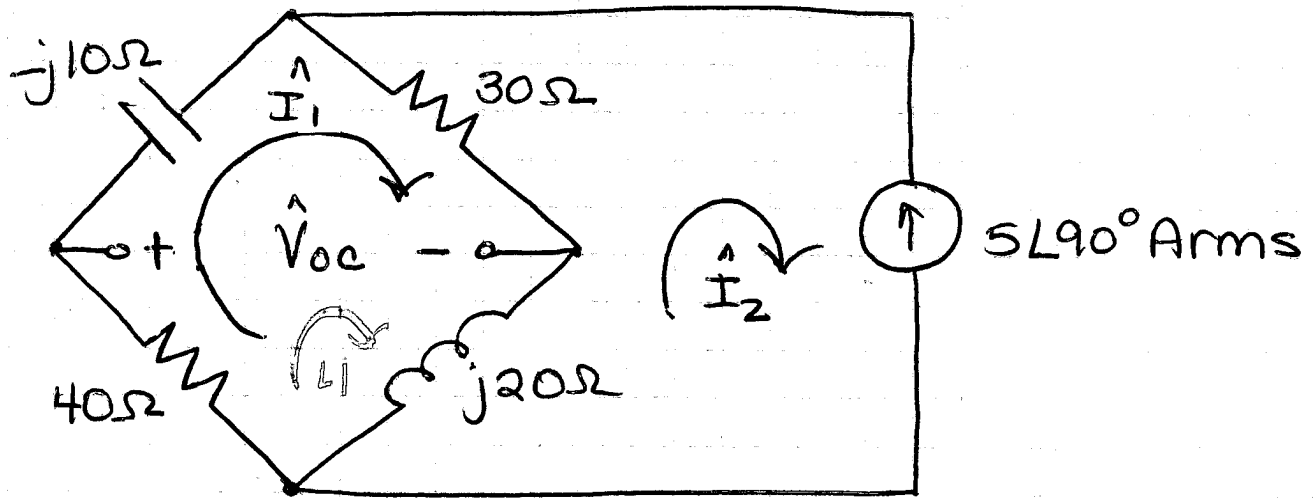


Extra Problems for Exam II

Solutions

①

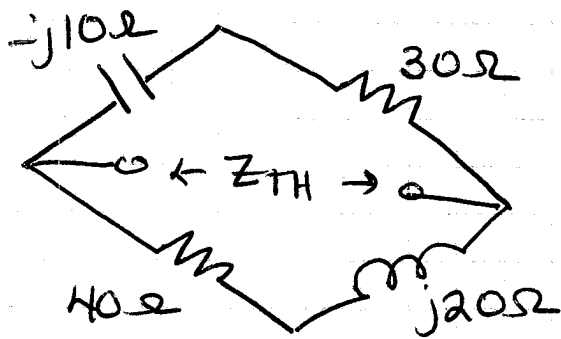


$$\hat{I}_2 = 5 \angle -90^\circ \text{ Arms} \quad -(40 - j10)\hat{I}_1 - (30 + j20)(\hat{I}_1 - \hat{I}_2) = 0$$

$$\hat{I}_1 = 2.55 \angle -64.44^\circ \text{ Arms}$$

KVL at L1: $-40\hat{I}_1 - \hat{V}_{oc} - j20(\hat{I}_1 - \hat{I}_2) = 0$

$$\hat{V}_{oc} = 70.72 \angle 81.89^\circ \text{ Vrms}$$



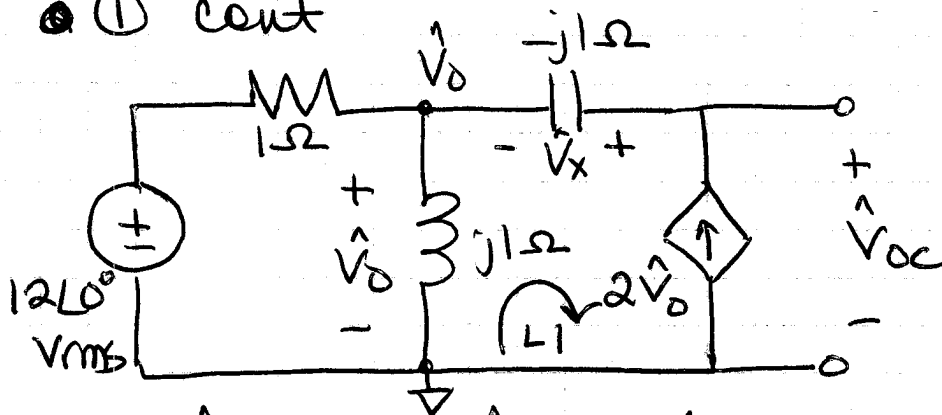
$$Z_{TH} = (30 - j10) \parallel (40 + j20)$$

$$= 20 \Omega$$

$$Z_L = 20 \Omega$$

$$P_L = 62.52 \text{ W, Abs}$$

① cont



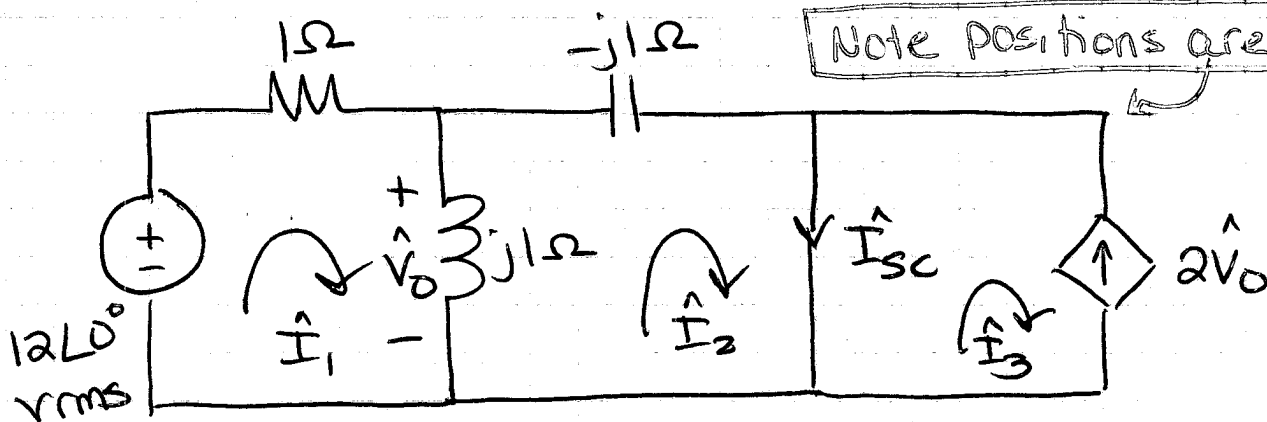
$$\frac{\hat{V}_0 - 12}{1} + \frac{\hat{V}_0}{j1} - 2\hat{V}_0 = 0$$

$$\hat{V}_0 = 8.48 \angle 35^\circ \text{ Vrms}$$

$$\hat{V}_x = 2\hat{V}_0(-j1)$$

by KVL: $\hat{V}_0 + \hat{V}_x - \hat{V}_{0c} = 0$

$$\hat{V}_{0c} = 18.97 \angle 71.57^\circ \text{ Vrms}$$



Note positions are switched

know: $\hat{V}_0 = j1(\hat{I}_1 - \hat{I}_2)$

$$\hat{I}_{sc} = \hat{I}_2 - \hat{I}_3$$

$$12\angle 0^\circ - \hat{I}_1 - j1(\hat{I}_1 - \hat{I}_2) = 0$$

$$\hat{I}_3 = -2\hat{V}_0 = j2(\hat{I}_2 - \hat{I}_1)$$

$$-j1(\hat{I}_2 - \hat{I}_1) - (-j1)\hat{I}_2 = 0$$

$$\hat{I}_3 = 24 \angle 80^\circ \text{ Arms}$$

$$\hat{I}_1(-1-j1) + \hat{I}_2(j1) = -12$$

$$\hat{I}_{sc} = 26.83 \angle 26.56^\circ \text{ Arms}$$

$$\hat{I}_1(j1) + \hat{I}_2(0) = 0$$

$$Z_{TH} = 0.707 \angle 45^\circ \Omega$$

$$\hat{I}_1 = 0 \quad \hat{I}_2 = 12 \angle 90^\circ$$

$$Z_L = 0.707 \angle -45^\circ \Omega$$

pg 3 Ex Prob Exam 2

① cont

$$P_L = \left(\frac{18.97}{1} \right)^2 (.5) = 179.90 \text{ W, Abs}$$

②

a) $Z_1: \hat{I}_1 = 66.67 \angle -63.26^\circ \text{ Arms}$

$$Z_1 = 1.5 \angle 63.26^\circ \Omega$$

$$Z_2: \hat{I}_2 = 120 \angle -80^\circ \text{ Arms}$$

$$Z_2 = 0.833 \angle 80^\circ \Omega$$

$$Z_3: \hat{I}_3 = 109.11 \angle -66.42^\circ \text{ Arms}$$

$$Z_3 = 0.92 \angle 66.42^\circ \Omega$$

b) $\hat{I}_S = 293.35 \angle -71.21^\circ \text{ Arms}$

c) $P_S = 9.45 \text{ kW}$

d) $\hat{S}_S = 29.34 \angle 71.21^\circ \text{ kVA}$

e) $\text{pf}_{1-3} = \cos(71.21) = 0.322 \text{ lag}$

f) $\hat{I}_{S\text{new}} = 99.46 \angle -18.19^\circ \text{ Arms}$

$$\hat{I}_C = 246.67 \angle 90^\circ \text{ Arms}$$

$$Z_C = 0.405 \angle -90^\circ \Omega \quad \text{or } C = 6.55 \text{ mF}$$

g) For $\text{pf} = 1$ $\hat{I}_{S\text{new}} = 94.50 \angle 0^\circ \text{ Arms}$

max reduction is $\sim 70\%$

③ Omit this problem. (I didn't give enough info)

④ a) $\hat{V}_{an} = 259.81 \angle 0^\circ \text{ Vrms}$
 $\hat{V}_{ab} = 450 \angle 30^\circ \text{ Vrms.}$

b) Assume Y-Y system

$Z_{Y1} : \hat{I}_{Y1} = 47.37 \angle -49.5^\circ \text{ Arms } (Z_{Y1} = 5.48 \angle 49.5^\circ \Omega)$

$Z_{Y2} : \hat{I}_{Y2} = 19.25 \angle -60^\circ \text{ Arms } (Z_{Y2} = 40.49 \angle 60^\circ \Omega)$

$Z_{Y3} : \hat{I}_{Y3} = 50.18 \angle -57.53^\circ \text{ Arms}$
 $(Z_{Y3} = 15.50 \angle 57.53^\circ \Omega)$

$\hat{I}_{aA} = 116.46 \angle -54.68^\circ \text{ Arms}$

c) In Y-Y : $V_p = 259.81 \text{ Vrms}$
 $I_p = 116.46 \text{ Arms}$

In Y- Δ : $V_p = 450 \text{ Vrms}$
 $I_p = 67.24 \text{ Arms}$

d) $\hat{S}_s = 90.77 \angle 54.68^\circ \text{ kVA}$

e) $|\hat{I}_{aA\text{new}}| = 58.23 \text{ Arms } P_s = 52.5 \text{ kW}$

$\text{pf}_{CL} = 1.156 \Rightarrow \text{No such load exists!}$

best $\text{pf}_{CL} = 1 \quad |\hat{I}_{aA\text{new}}| = 67.36 \text{ Arms}$

$\hat{I}_{aA\text{new}} = 67.36 \angle 0^\circ \text{ Arms } Z_{yc} = 2.73 \angle -90^\circ \Omega$

pg 5

④ cont $Z_{\Delta C} = 8.20 \angle -90^\circ \Omega$

⑤ Assume $\gamma-\gamma$ first

$$LZ_{Y1-3} = 25.84^\circ \quad \hat{I}_{aA} = 116.39 \angle -25.84^\circ \text{ Arms}$$

$$\hat{V}_{an} = 120.09 \angle 0^\circ \text{ Vrms}$$

$$\hat{V}_{ab} = 208 \angle 30^\circ \text{ Vrms}$$

$$\hat{S}_{3\phi_{1-3}} = \sqrt{3} V_L I_L \angle 25.84^\circ = 41.93 \angle 25.84^\circ \text{ kVA}$$

$$\hat{S}_{3\phi_1} = 22.5 \angle 36.87^\circ \text{ kVA}$$

$$\hat{S}_{3\phi_2} = 10 \angle 53.13^\circ \text{ kVA}$$

$$\left. \begin{array}{l} \hat{S}_{3\phi_1} \\ \hat{S}_{3\phi_2} \end{array} \right\} \text{sum} \Rightarrow \hat{S}_{3\phi_{1-2}} = 32.22 \angle 41.86^\circ \text{ kVA}$$

$$\hat{S}_{3\phi_3} = \hat{S}_{3\phi_{1-3}} - \hat{S}_{3\phi_{1-2}} = 14.11 \angle -13.21^\circ \text{ kVA}$$

$$14.11 \times 10^3 = \sqrt{3} V_L I_{Y3} \Rightarrow \hat{I}_{Y3} = 39.18 \angle 13.21^\circ \text{ kVA}$$

$$I_{Y3} = 39.18 \text{ Arms}$$

⑥ $Z_{Y3} = 3.06 \angle -13.21^\circ \Omega$

c) $\hat{S}_{3\phi_3} = 14.11 \angle -13.21^\circ \text{ kVA}$

⑦ $Z_{\Delta 3} = 9.20 \angle -13.21^\circ \Omega$

⑧ $P_{3\phi} = 13.74 \text{ kW}$

⑥ a) lagging $Q_L > 0$

b) $Q_{3\phi} = 6 \text{ kVAR}$ $\text{pf} = 0.5 \text{ lag}$ $LZ_{\Delta} = 60^\circ$

$$I_L = 25 \text{ Arms}$$

pg 6

(6) cont

b) $Q_{3\phi} = \sqrt{3} V_L I_L \sin(60^\circ)$

$$V_L = 160 \text{ Vrms}$$

$$\hat{V}_{an} = 92.38 \angle 0^\circ \text{ Vrms}$$

c) $\hat{V}_{ab} = 160 \angle 30^\circ \text{ Vrms}$

d) $I_p = \frac{I_L}{\sqrt{3}} = 14.33 \text{ Arms}$

e) $\hat{S}_{3\phi} = \sqrt{3} (160)(25) \angle 60^\circ$
 $= 6.93 \angle 60^\circ \text{ kVA}$

f) $P_{3\phi} = 3.465 \text{ kW}$ $|\hat{I}_{aA}|_{\text{new}} = 20 \text{ Arms}$

Assume
Y-Y

$$3.465 \times 10^3 = \sqrt{3} (160)(20) \text{ pf}_{\text{new}} \quad \text{pf}_{\text{new}} = 0.625 \text{ lag}$$

$$\angle Z_{YCL} = \cos^{-1}(0.625) = 51.31^\circ$$

$$\hat{I}_{aA \text{ new}} = 20 \angle -51.31^\circ \text{ Arms}$$

$$\hat{I}_{cy} = (20 \angle -51.31^\circ) - (25 \angle -60^\circ)$$
$$= 6.04 \angle 90^\circ \text{ Arms}$$

$$\boxed{Z_{cy} = 15.29 \angle -90^\circ \Omega}$$